

$$2\operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x$$

$$2 \cdot \frac{\sin x}{\cos x} + \frac{\sin 2x}{\cos 2x} = \frac{\sin 4x}{\cos 4x}$$

$$2 \cdot \frac{\sin x}{\cos x} + 2 \cdot \frac{\sin x \cdot \cos x}{\cos 2x} = 2 \cdot \frac{\sin 2x \cdot \cos 2x}{\cos 4x}$$

$$2 \cdot \frac{\sin x}{\cos x} + 2 \cdot \frac{\sin x \cdot \cos x}{\cos 2x} = 4 \cdot \frac{\sin x \cdot \cos x \cdot \cos 2x}{\cos 4x}$$

$$\frac{\sin x}{\cos x} + \frac{\sin x \cdot \cos x}{\cos 2x} - 2 \cdot \frac{\sin x \cdot \cos x \cdot \cos 2x}{\cos 4x} = 0$$

$$\frac{\sin x}{\cos x} + \frac{\sin x \cdot \cos x}{\cos 2x} - 2 \cdot \frac{\sin x \cdot \cos x \cdot \cos 2x}{\cos 4x} = 0$$

$$\frac{\sin x}{\cos x} + \frac{\sin x \cdot \cos x}{\cos 2x} - 2 \cdot \frac{\sin x \cdot \cos x \cdot \cos 2x}{\cos 4x} = 0$$

$$1) \sin x = 0$$

$$2) \frac{1}{\cos x} + \frac{\cos x}{\cos 2x} - 2 \cdot \frac{\cos 2x}{\cos 4x} = 0$$

$$1) x = Pn$$

$$2) \frac{1}{\cos x} + \frac{\cos x}{\cos 2x} - 2 \cdot \frac{\cos 2x}{\cos 4x} = 0$$

$$\frac{(\cos 2x + \cos x^2)}{\cos x \cdot \cos 2x} - 2 \cdot \frac{\cos 2x \cdot \cos x}{\cos 4x} = 0$$

$$\frac{(2 \cos^2 x - 1 + \cos^2 x)}{\cos x \cdot (2 \cos^2 x - 1)} - 2 \cdot \frac{\cos x (2 \cos^2 x - 1) \cdot \cos x}{(2 \cos^2 x - 1)^2} = 0$$

$$\frac{(3 \cos^2 x - 1)}{(2 \cos^2 x - 1)^2} - 2 \cdot \frac{\cos x (2 \cos^2 x - 1) \cdot \cos x}{(2 \cos^2 x - 1)^2} = 0$$

$$\cos x \neq 0$$

$$\cos 2x \neq 0$$

$$\cos 4x \neq 0$$

$$\cos x \neq 0$$

$$x \neq P/2 + Pn$$

$$\cos 2x \neq 0$$

$$2x \neq P/2 + Pn$$

$$x \neq P/4 + Pn/2$$

$$\cos 4x \neq 0$$

$$4x \neq P/2 + Pn$$

$$x \neq P/8 + Pn/4$$

2 путь

$$2\operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x$$

$$\operatorname{tg}x + \operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x$$

$$\operatorname{tg}x + \operatorname{tg}2x = \operatorname{tg}4x - \operatorname{tg}x$$

Преобразуем все в sin/cos и т д

$$\frac{\sin x}{\cos x} + \frac{\sin 2x}{\cos 2x} = \frac{\sin 4x}{\cos 4x} - \frac{\sin x}{\cos x}$$

$$\frac{(\sin x \cdot \cos 2x + \sin 2x \cdot \cos x)}{\cos x \cdot \cos 2x} = \frac{(\sin 4x \cdot \cos x - \sin x \cdot \cos 4x)}{\cos x \cdot \cos 4x}$$

$$\frac{\sin(x+2x)}{\cos x \cdot \cos 2x} = \frac{\sin(4x-x)}{\cos x \cdot \cos 4x}$$

$$\frac{\sin 3x}{\cos x \cdot \cos 2x} = \frac{\sin 3x}{\cos x \cdot \cos 4x}$$

$$\frac{\sin 3x}{\cos x} \cdot \frac{1}{\cos 2x} = \frac{\sin 3x}{\cos x} \cdot \frac{1}{\cos 4x}$$

$$\frac{\sin 3x}{\cos x} \cdot \frac{1}{\cos 2x} - \frac{\sin 3x}{\cos x} \cdot \frac{1}{\cos 4x} = 0$$

$$\frac{\sin 3x}{\cos x} = 0$$

$$\sin 3x = 0$$

$$3x = Pn$$

$$x = Pn/3$$

$$\frac{1}{\cos 2x} - \frac{1}{\cos 4x} = 0$$

$$\frac{(\cos 4x - \cos 2x)}{\cos 2x \cdot \cos 4x} = 0$$

$$\cos 4x - \cos 2x = 0$$

$$2 \cos^2 2x - 1 - \cos 2x = 0$$

$$\cos 2x = y$$

$$2y^2 - y - 1 = 0$$

$$y_1 = \frac{1+3}{4} = 1$$

$$y_2 = \frac{1-3}{4} = -\frac{1}{2}$$

$$\cos 2x = 1$$

$$2x = 2Pn$$

$$x = Pn$$

$$\cos 2x = -\frac{1}{2}$$

$$2x = 2P/3 + 2Pn$$

$$2x = 4P/3 + 2Pn$$

$$x_1 = P/3 + Pn$$

$$x_2 = 2P/3 + Pn$$

Ответ:  $Pn/3$ ;

$$P/8 + P/4 > P/3$$

